

Augmenting treatment arms with external data through propensity-score weighted power-priors: an application in expanded access

Tobias Polak^{1,2,3,4}, Jeremy Labrecque², Carin Uyl-de Groot⁴,
Joost van Rosmalen^{1,2}

¹Department of Biostatistics, Erasmus MC, Rotterdam, the Netherlands

²Department of Epidemiology, Erasmus MC, Rotterdam, the Netherlands

³RWD Department, myTomorrows, Amsterdam, The Netherlands

⁴Erasmus School of Health & Policy Management, Rotterdam, the Netherlands

Bayes Pharma 2023

Introduction

- Leveraging information from **external controls** can improve power and precision of a clinical trial.
- Classically, methods have focused on using **historical controls** (Pocock 1976).
- In recent years, increasing interest in using **real-world data** (RWD).
- Methods focused mostly on external controls, not on external treatment arms.

Introduction

Pocock's criteria for suitability of historical controls:

- Same treatment
- Historical trial is a recent clinical study
- Same requirements for patient eligibility
- Same methods of treatment evaluation
- Comparable distributions of important patient characteristics
- Trials performed in the same organization
- No other reasons to expect different results

Introduction

- Two sources of potential **bias** when including external data in RCT:
 - Measured confounding
 - Unmeasured confounding
- **Bayesian dynamic borrowing methods** mitigate unmeasured confounding by downweighting external data.
- **Main methods**: power prior, meta-analytic-predictive prior, commensurate prior (Viele et al. Pharm Stat 2014)
- Informative prior for analysis of RCT, based on external controls
- Covariate adjustment or propensity score methods to account for measured confounding

Introduction

- When borrowing historical controls, patient characteristics should be comparable (Pocock's criteria).
- This assumption is not plausible when borrowing RWD.
- Few **hybrid methods** that can adjust for both sources of bias.
- **Goal of new method**: provide a double safeguard against measured and unmeasured confounding when combining RWD with trial data

Hybrid methods

Hybrid methods developed so far:

- Wang et al. (J Biopharm Stat 2019): power prior with propensity score stratification
- Liu et al. (Stat Med 2021): meta-analytic predictive prior with propensity score stratification
- Wang et al. (J Biopharm Stat 2022) reviewed several methods and proposed propensity weighting with fixed and commensurate priors

Disadvantages of most of these methods:

- Fixed number of external patients to be borrowed
- Many parameters/settings to be chosen for implementation

Vemurafenib application

- **Expanded access:** pathway of non-trial access to investigational medicine for patients with seriously debilitating or life-threatening illnesses
- Expanded access data are a source of RWD.
- **Motivating example:** Vemurafenib is a drug approved for late-stage melanoma harboring a V600E BRAF mutation.
- **Data:** single-arm phase II study (n=132) and expanded access program (n=241)
- **Primary endpoint:** objective response rate

Vemurafenib application

Patient characteristics of vemurafenib case study

Characteristic	Clinical Program	
	Expanded access, N = 241 ¹	Trial, N = 132 ¹
Age at enrolment	53 (13)	50 (15)
Gender assigned at birth		
Female	95 (39%)	51 (39%)
Male	146 (61%)	81 (61%)
Melanoma stage		
M1a	22 (9.1%)	33 (25%)
M1b	26 (11%)	18 (14%)
M1c	182 (76%)	80 (61%)
Unresectable Stage III	11 (4.6%)	0 (0%)
ECOG performance status		
Grade 0	112 (46%)	61 (46%)
Grade 1	98 (41%)	71 (54%)
Grade 2	30 (12%)	0 (0%)
Grade 3	1 (0.4%)	0 (0%)
Objective response rate	129 (54%)	75 (57%)

¹ Mean (SD); n (%)

Power prior

- **Power prior**: Bayesian method for borrowing external data
- Formulation: $p(\theta | \mathcal{Y}, \delta) \propto \mathcal{L}(\theta | \mathcal{Y}_0) \mathcal{L}(\theta | \mathcal{Y}_e)^\delta \pi(\theta)$, where δ is weight of external data, with $0 \leq \delta \leq 1$.
- **Modified power prior (MPP)**: estimate weight based on available data (Duan et al. 2005):

$$p(\theta, \delta | \mathcal{Y}) \propto \mathcal{L}(\theta | \mathcal{Y}_0) \mathcal{L}(\theta | \mathcal{Y}_e)^\delta \frac{1}{C(\delta)} \pi(\delta) \pi(\theta)$$

- $C(\delta) = \int_{\theta} \mathcal{L}(\theta | \mathcal{D}_e)^\delta \pi(\theta) d\theta$ is a scaling constant to ensure the MPP abides by the **likelihood principle**.

Propensity scores

- Propensity score methods typically used to address biases due to confounding in non-randomized experimental settings.
- Here we use propensity scores to model the allocation between current and external data (Z), with $\lambda_i = \Pr(Z = 1 \mid \mathcal{X} = x_i)$, following Lin et al. (Pharm Stat 2018).

Integrating propensity scores and power prior

- **Main idea of proposed method (ProPP):** combine propensity score weights with likelihood of MPP.
- ProPP method uses RWD likelihood with:

$$\mathcal{L}(\theta | \mathcal{Y}_e)^\delta = \left(\prod_i f(y_i | \theta)^{w_i} \right)^\delta$$

- Weight w_i chosen as function of the propensity score λ_i .
- Effective weight for patient i : $\delta \times w_i$.

Integrating propensity scores and power prior

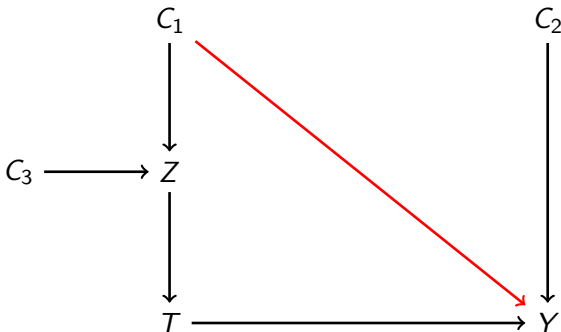
- Estimand is **average treatment effect of the trial**.
- Weights > 1 are not desirable:
 - Inflated sample size in Bayesian analysis would lead to overestimation of precision.
 - Weighting a non-trial participant higher than trial participants may not be acceptable to regulators.
- We set $w_i = 1$ for trial population and $w_i = \min\left(1, \frac{\lambda(x)}{1-\lambda(x)}\right)$ for external data.

Propensity score weighting schemes under different populations of interest

Trial	External	Population of interest
$\frac{1}{\lambda(x)}$	$\frac{1}{1-\lambda(x)}$	Average treatment effect
1	$\frac{\lambda(x)}{1-\lambda(x)}$	Average treatment effect of the trial
$\frac{1-\lambda(x)}{\lambda(x)}$	1	Average treatment effect of the external

Causal interpretation

Directed acyclic graph to explore the causal implications of the ProPP

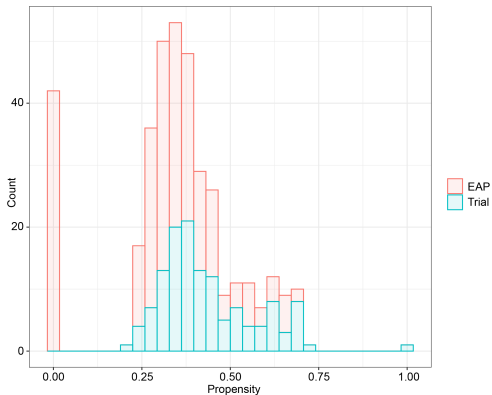


Implementation

- ProPP method applied for dichotomous outcomes
- Closed-form expressions for marginal posterior of δ and conditional posterior of θ given δ
- Easy posterior sampling using [rejection sampling](#) (no need for MCMC)

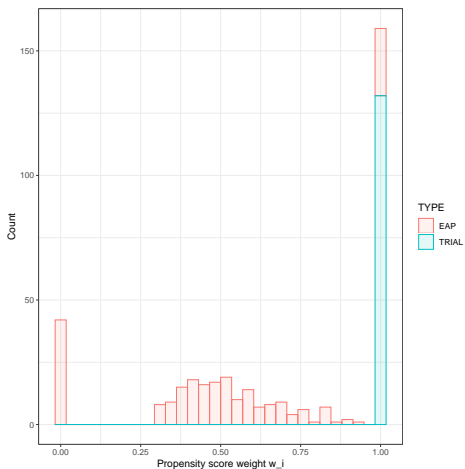
Vemurafenib application

Distribution of propensity scores in trial and expanded access program



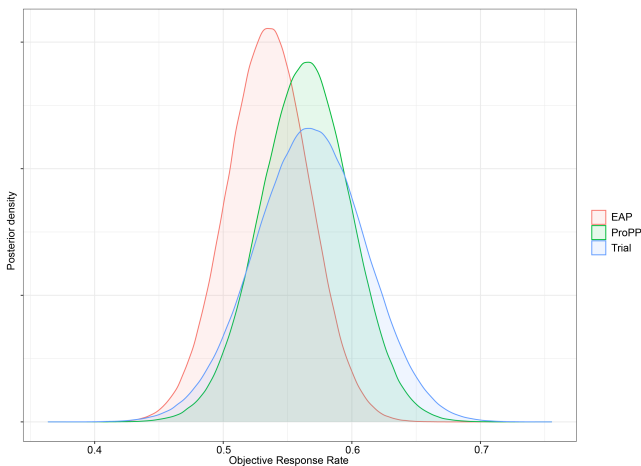
Vemurafenib application

Distribution of weights w_i in trial and expanded access program



Vemurafenib application

Inclusion of expanded access data increases precision of posterior estimates



Simulation study

- Simulation study to assess performance of ProPP in terms of type I error rate and RMSE
- Data of dichotomous outcome simulated using

$$\text{logit } y_i | x_i, z_i = \beta_0 + \beta x_i + \eta \times I(z_i = 1)$$

- β_0 is intercept, β is row vector of coefficients and η is drift term.

Simulation study

- **Base case setting:** $N_0 = 400$ in the trial, $N_e = 400$ in the external data, $K = 5$ different continuous covariates X with $\beta_j = 0.1$, $j = 1, \dots, 5$ and $\beta_0 = 0$.
- Patient characteristics in trial: $X_0 \sim \mathcal{N}(\mu_0, \sigma_0^2)$
- Patient characteristics in external data:
 $X_e \sim (1 - \psi)\mathcal{N}(\mu_e, \sigma_e^2) + \psi\mathcal{N}(\mu_0, \sigma_0^2)$
- **Degree of overlap** (ψ) varied in simulations

Simulation study

- **Two scenarios:**

- **Drift:** bias due to variation in η , with $\eta \in [-0.5, 0.5]$ and $X_e, X_0 \sim N(0, 1)$ and $\beta = 0$ (no effect of covariates).

- **Mixture:** bias due to variation in covariate distributions (patient characteristics), with $\beta = 0.1$.

The covariates come from a mixture distribution with $\psi = 0.5$.

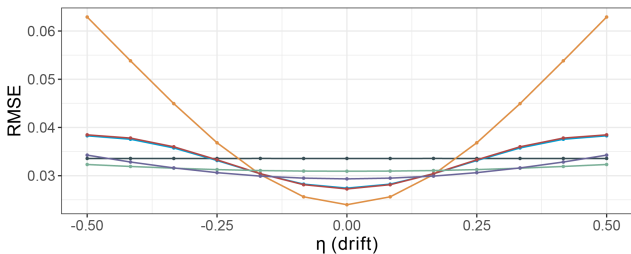
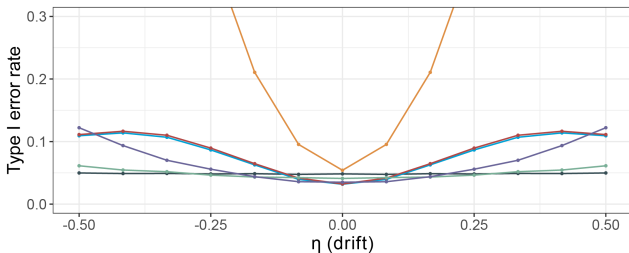
We assume $X_0 \sim \mathcal{N}(0, 1)$ and we vary mean of RWD $\mu_e \in [-0.5, 0.5]$.

There is no drift, $\eta = 0$.

- **Parameter of interest:** baseline rate in trial, β_0 .

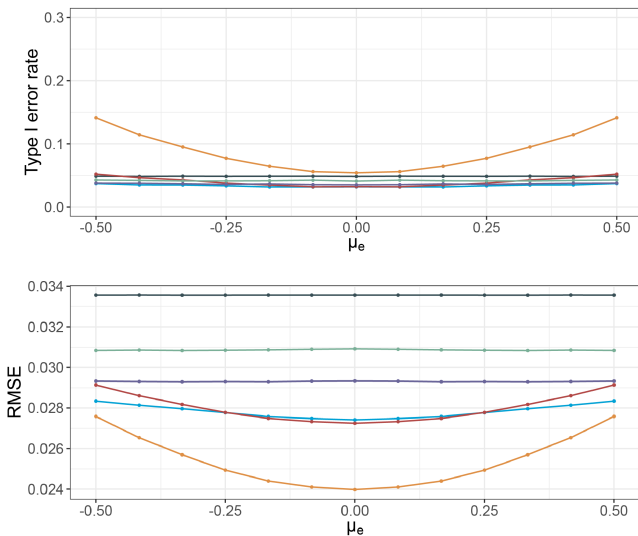
- ProPP method compared with:
 - Ignore (no RWD)
 - Pooling (combining without adjustment)
 - Modified power prior
 - Stratification + power-prior method suggested by Wang et al. (2019) with 10% or 20% borrowing of RWD

Simulation study: results of Drift scenario



Method — Ignore — Pooling — ProPP — MPP — Wang 10% — Wang 20%

Simulation study: results of Mixture scenario



Method — Ignore — Pooling — ProPP — MPP — Wang 10% — Wang 20%

Discussion

- ProPP compares favorably with traditional and novel methods in terms of RMSE and type-I error rate.
- Expanded access can be an important source of RWD.
- ProPP uses frequentist and Bayesian methodology to combine propensity score and dynamic borrowing methods.
- No **pre-elicitation of a fixed power parameter** or a **fixed amount of external patients** to be borrowed, but also no 'outcome-free' design.

Discussion

- Limiting the weights to a maximum of 1 may not capture all measured confounding.
- ProPP can be extended to time-to-event or normally distributed outcomes.
- Inclusion of RWD sources remains a trade-off between bias due to including non-trial data and increased precision due to increased sample size.
- ProPP allows to augment treatment arms with expanded access data in a prudent manner.