

# Assurance methods for designing a survival trial with a delayed treatment effect

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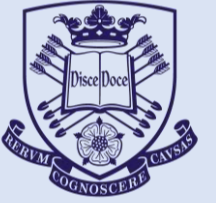
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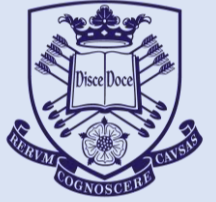




# Introduction

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- Overview of assurance/probability of success
- Delayed treatment effects
- Assurance with DTEs



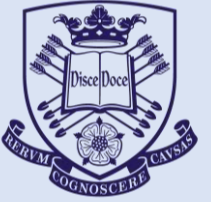
# What is assurance?

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- Power is

*“The probability of a trial being “successful” **given** a difference  $\theta$  exists”*

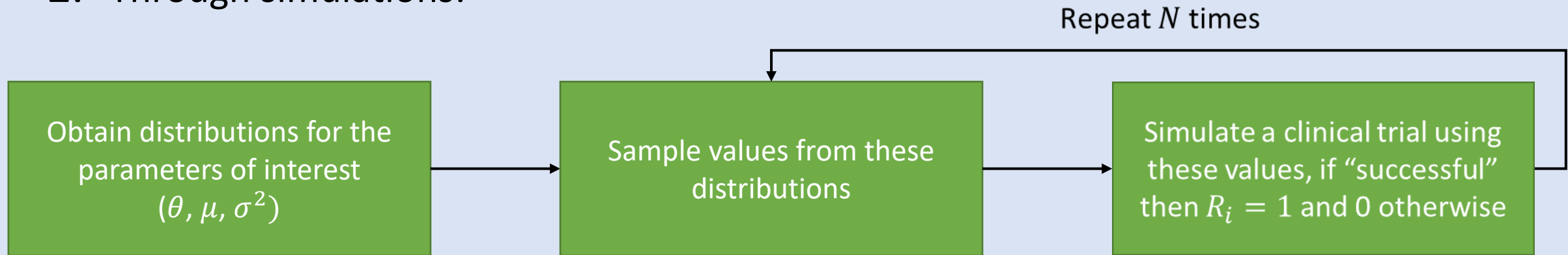
- However, this is **conditional**. Can we do better?
- If we obtain a prior distribution  $p(\theta)$  (instead of assuming  $\theta$  takes a fixed value), and integrate over this prior distribution then this probability is now **unconditional**
- This is called an **assurance calculation**<sup>1</sup>
- **Assurance** is also known as expected power, average power, predictive power, probability of success etc..



# How do you calculate assurance?

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- Two ways:
  1. Analytically
  2. Through simulations:

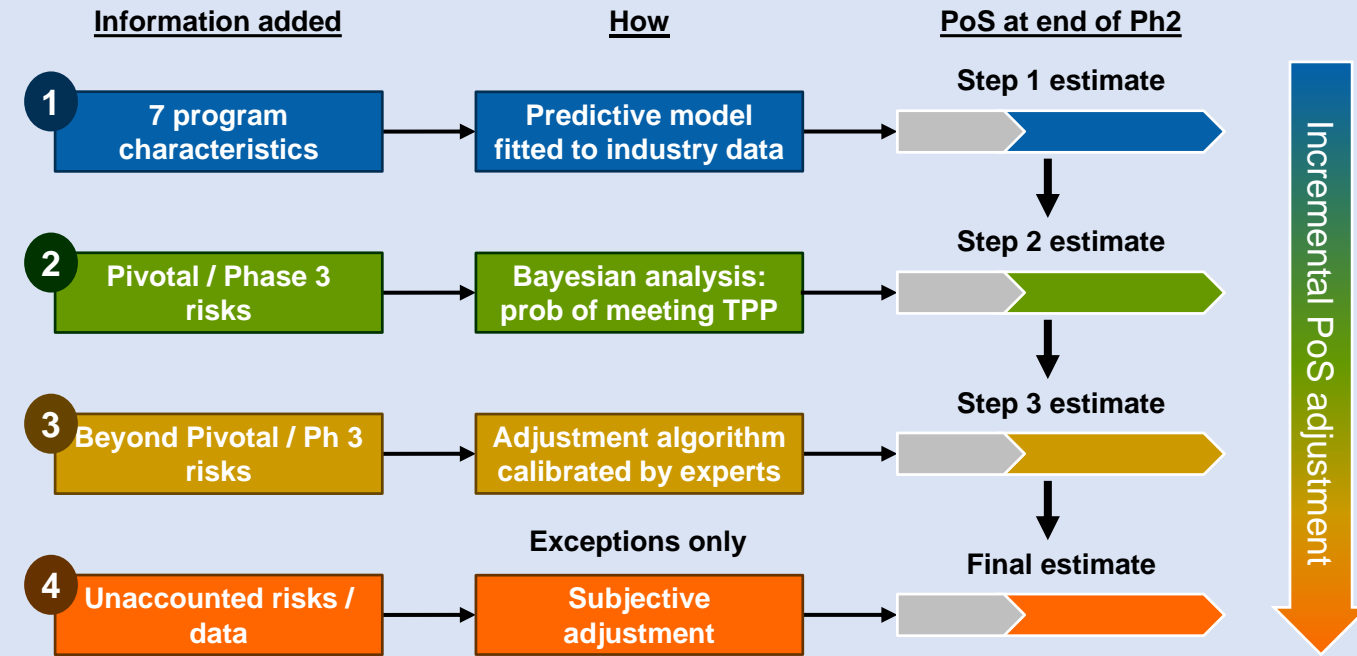
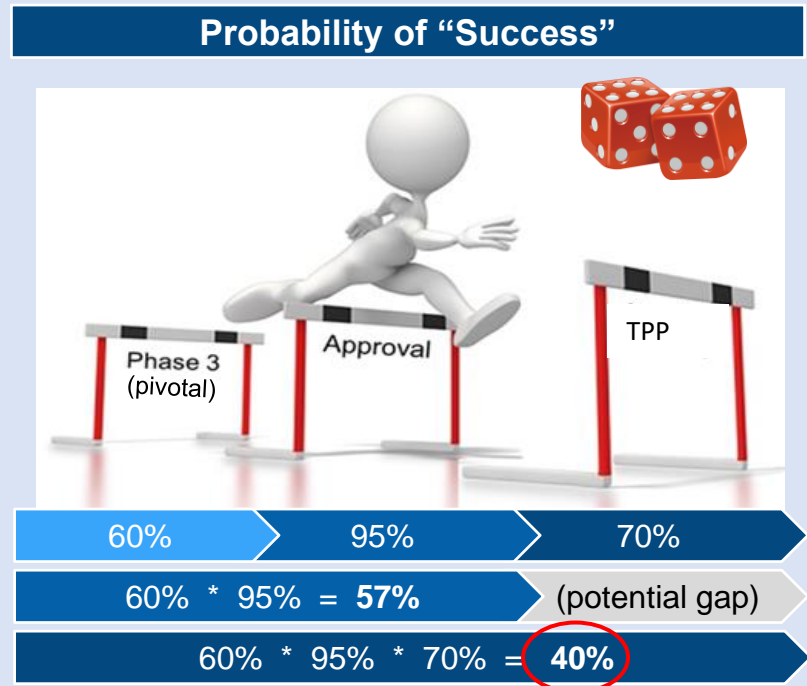


Assurance is then estimated as  $\hat{P}(R) = \frac{1}{N} \sum_{i=1}^N R_i$



# Probability of Success (PoS) at Novartis

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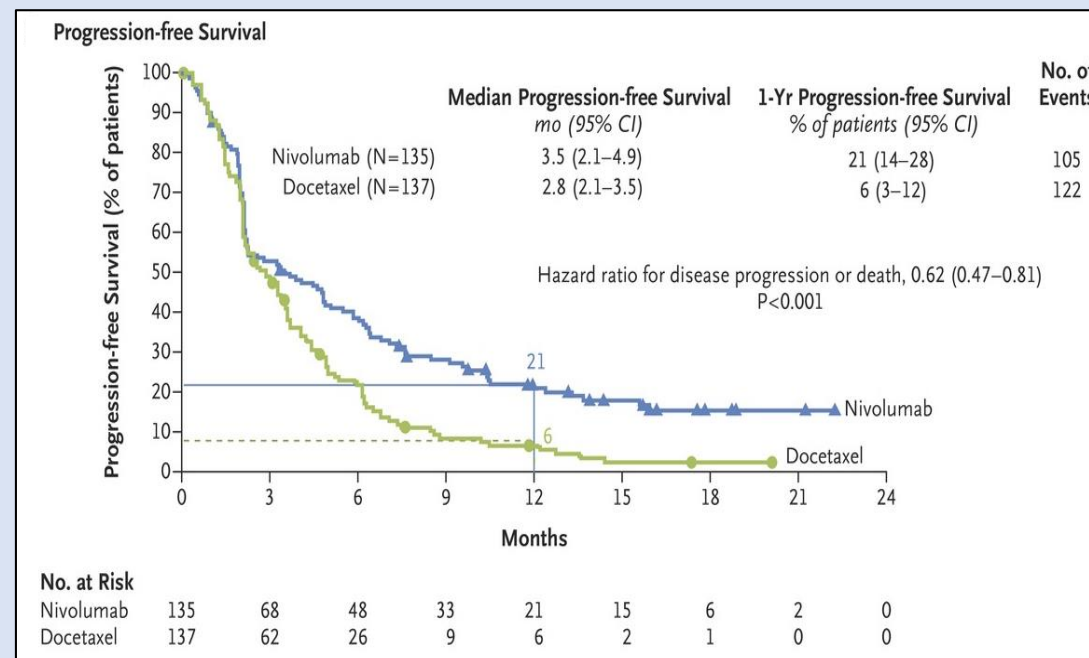
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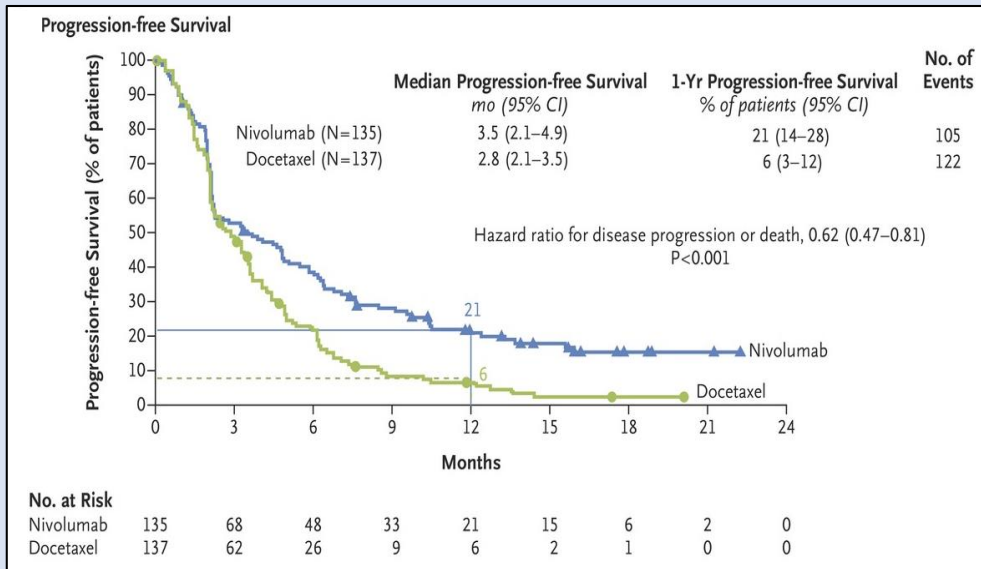


# Delayed Treatment Effects

- A survival trial in which the control and treatment survival arms follow the same trajectory for some time,  $T$ , at which time they separate
- This phenomenon is known as **delayed treatment effects (DTEs)** and is a form of **non-proportional hazards (NPHs)**

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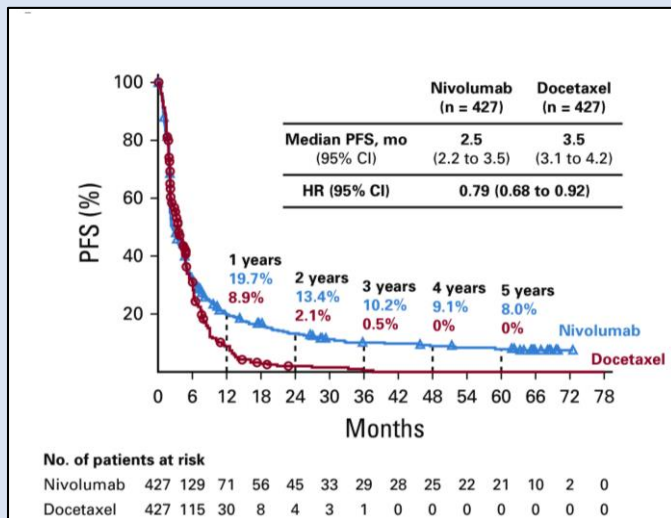
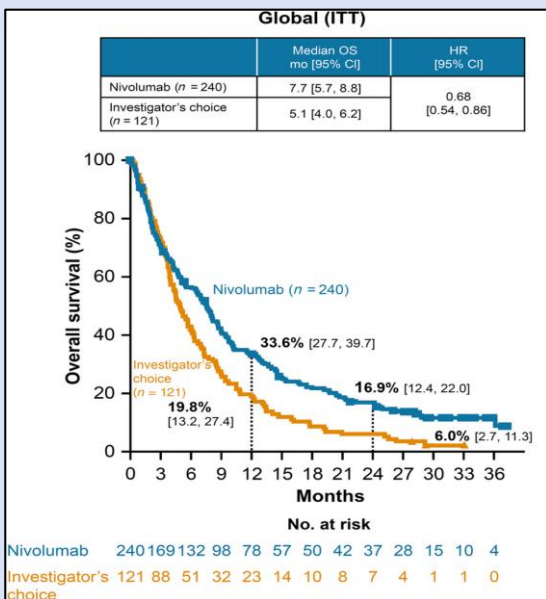
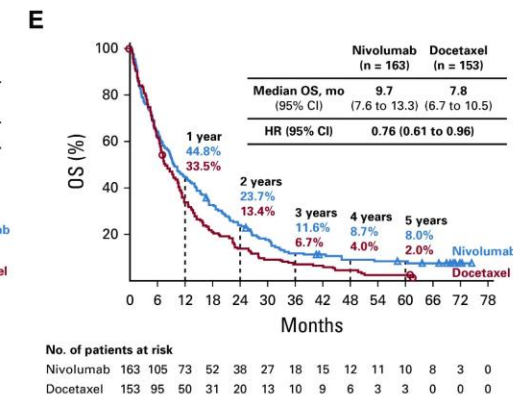
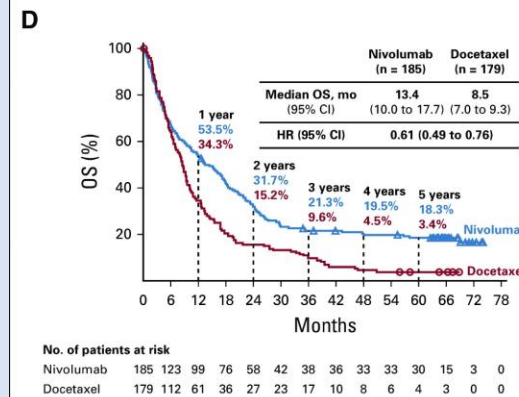
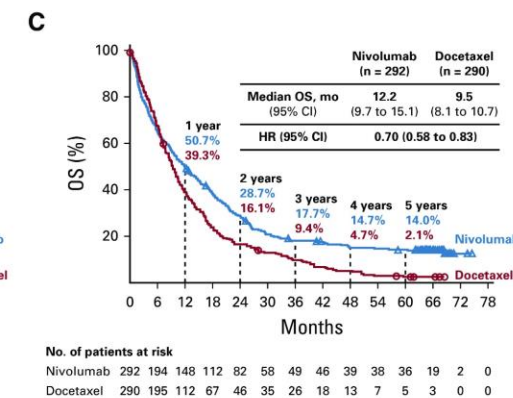
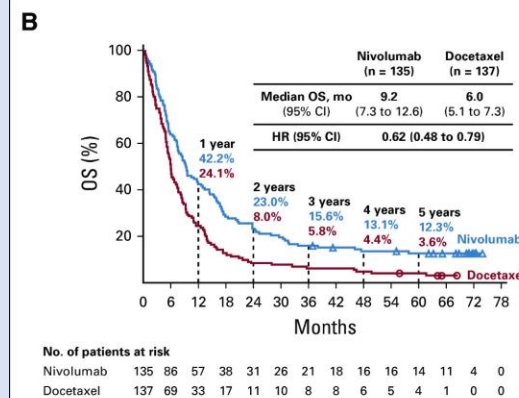
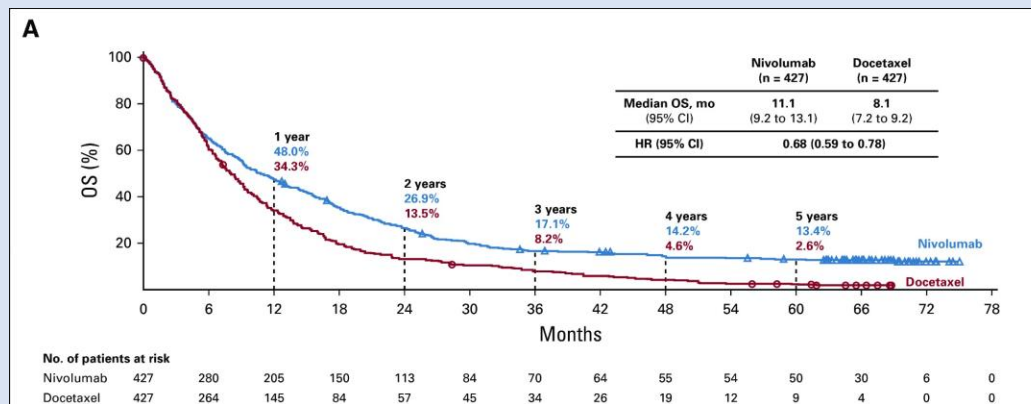


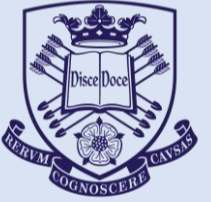


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# What makes DTE hard?

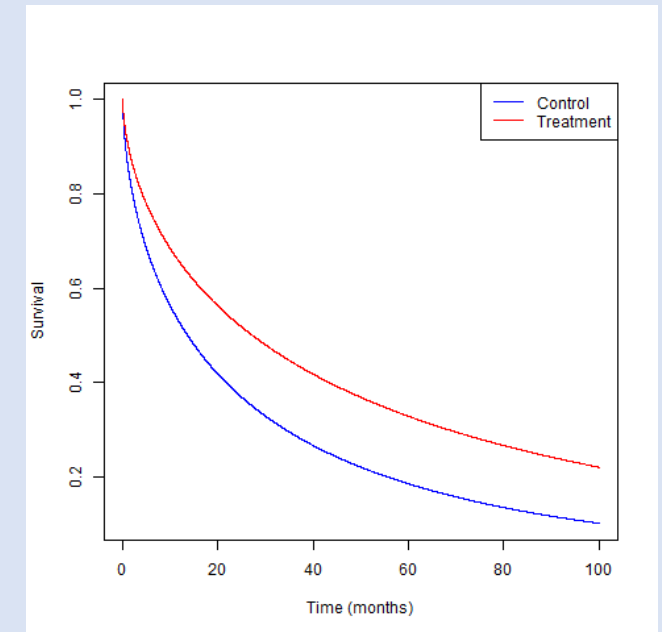
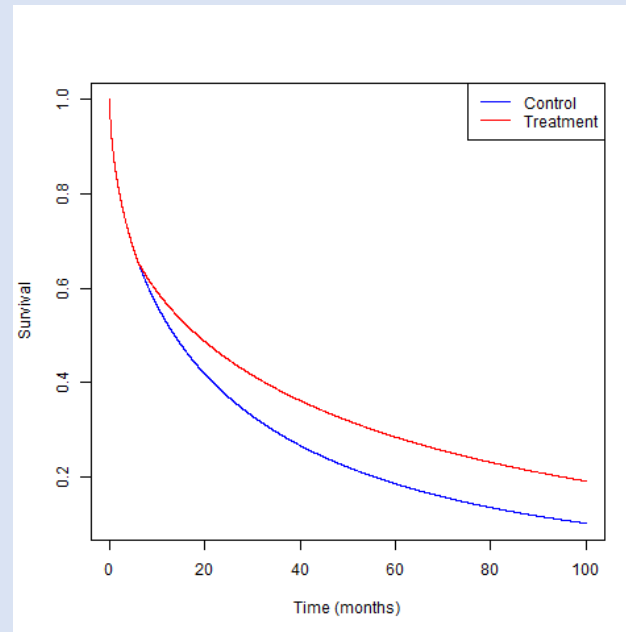
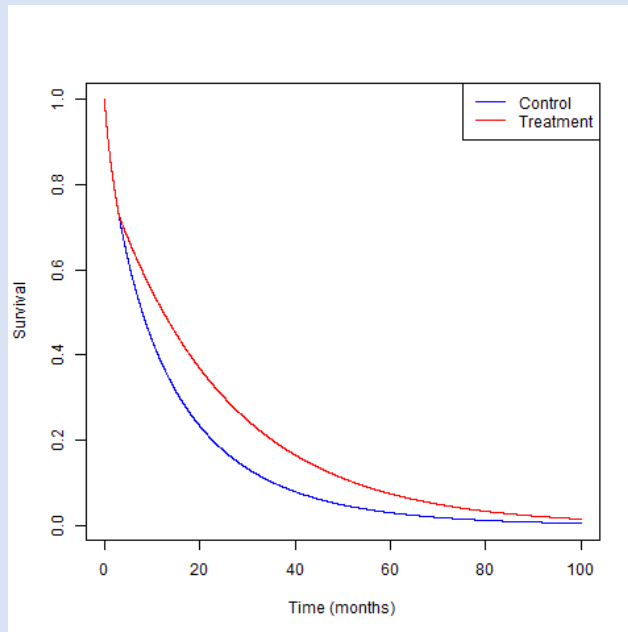
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- In design:
  - When are the curves going to separate?
  - If we don't account for the delay, we lose power
  - When to plan for interim analyses?
- In analysis:
  - Proportional hazards are violated, how to account for this?
  - Weighted log-rank test, RMST etc..



# Parameterisation

- $S_c(t) = \exp\{-(\lambda_c t)^{\gamma_c}\}$
- $S_t(t) = \begin{cases} \exp\{-(\lambda_c t)^{\gamma_c}\}, & 0 \leq t \leq T \\ \exp\{-(\lambda_c T)^{\gamma_c} - \lambda_t^{\gamma_t} (t^{\gamma_t} - T^{\gamma_t})\}, & t > T \end{cases}$





# Elicitation

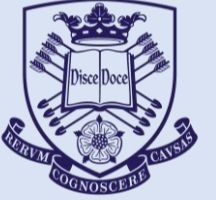
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- We have five unknown parameters in our parameterisation:  $\lambda_c, \gamma_c, \lambda_t, \gamma_t$  and  $T$
- How do we elicit beliefs about these parameters?
- For  $\lambda_c$  and  $\gamma_c$ :
  - We can use historical data (RBeST<sup>1</sup>)
  - Ren and Oakley (2014)<sup>2</sup> consider eliciting Weibull parameters
- For  $T$ :
  - We can ask questions directly about the length of delay
- For  $\lambda_t$  and  $\gamma_t$ :
  - We can ask questions such as:
    - Median survival time on experimental treatment
    - Survival probability at time  $t$
    - Hazard ratio at time  $t$

Slide 10

<sup>1</sup>Weber S, Li Y, Seaman JW, Kakizume T, Schmidli H (2021). "Applying Meta-Analytic-Predictive Priors with the R Bayesian Evidence Synthesis Tools." *\_Journal of Statistical Software\_*, \*100\*(19), 1-32. doi: 10.18637/jss.v100.i19

<sup>2</sup>Ren S, Oakley JE. Assurance calculations for planning clinical trials with time-to-event outcomes. *Stat Med*. 2014;33(1):31-45. doi:10.1002/sim.5916.



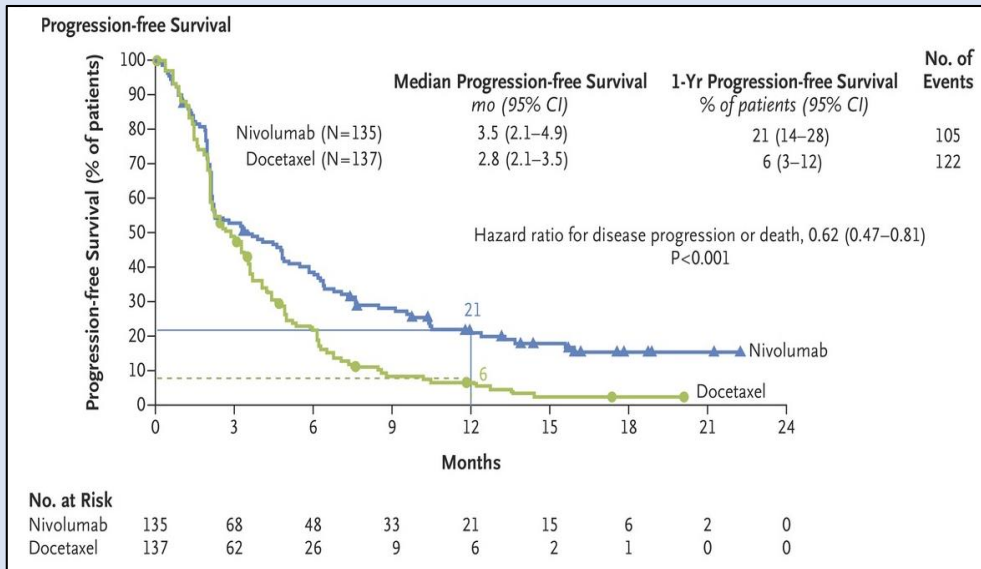
# Elicitation – hazard ratio

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- The **hazard ratio** is:

$$\text{HR}(t) \begin{cases} 1, & 0 \leq t \leq T \\ \frac{\gamma_t \lambda_t^{\gamma_t} t^{\gamma_t - 1}}{\gamma_c \lambda_c^{\gamma_c} t^{\gamma_c - 1}}, & t > T \end{cases}$$

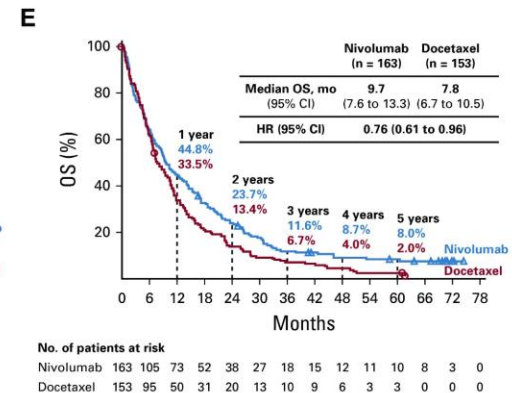
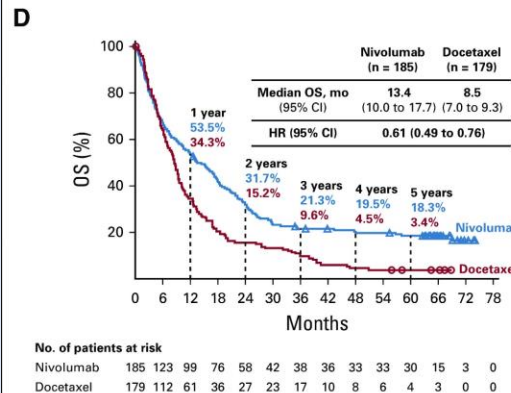
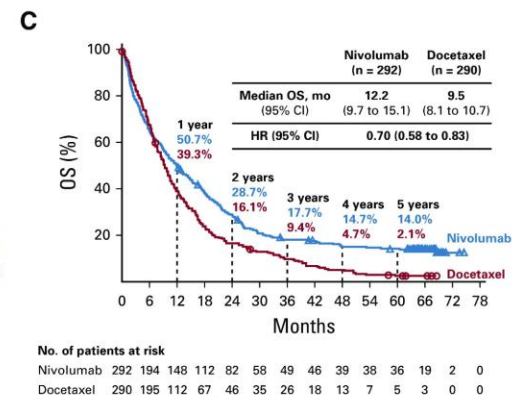
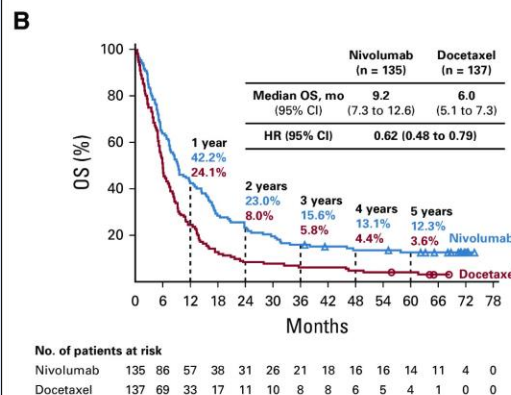
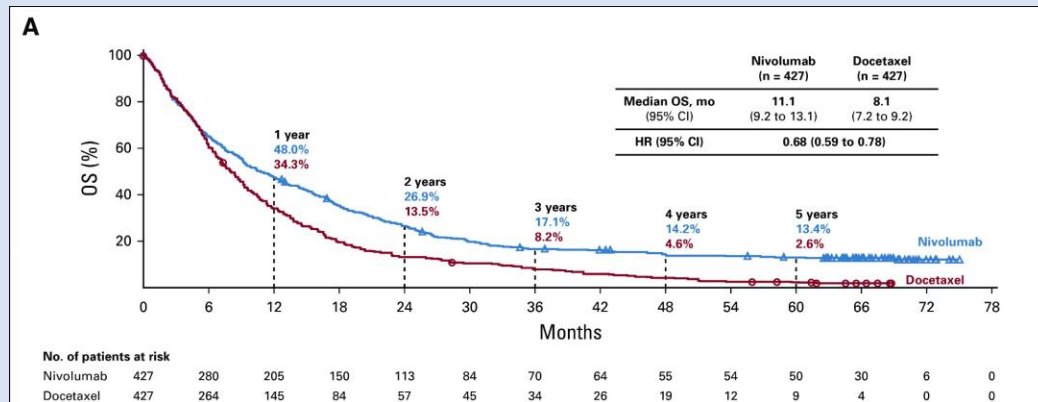
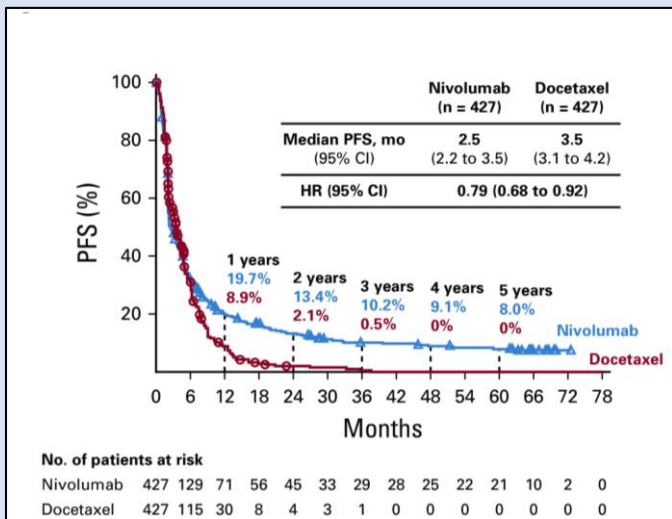
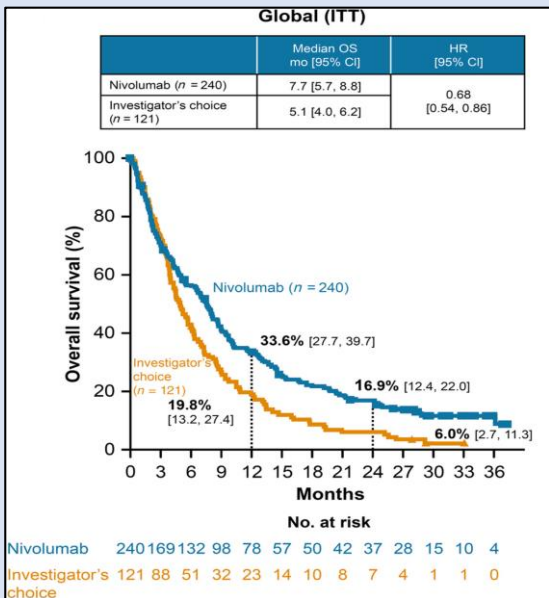
- We observe that after the delay, the hazard ratio seems to be **constant**

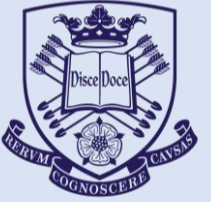


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# Elicitation – hazard ratio

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$$\text{HR}(t) \begin{cases} 1, & 0 \leq t \leq T \\ \frac{\gamma_t \lambda_t^{\gamma_t} t^{\gamma_t-1}}{\gamma_c \lambda_c^{\gamma_c} t^{\gamma_c-1}}, & t > T \end{cases}$$

- We observe that after the delay, the hazard ratio seems to be **constant**
- We incorporate this into the parameterisation by setting  $\gamma_c = \gamma_t$
- The post-delay HR ( $\text{HR}^*$ ) is now

$$\text{HR}^* = \left( \frac{\lambda_t}{\lambda_c} \right)^{\gamma_c}$$

- We are able to indirectly elicit beliefs about  $\lambda_t$  by asking questions about  $\text{HR}^*$



# Elicitation methods - SHELF

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- How do you actually elicit beliefs from experts? Non-trivial..
- **SH**effield **EL**icitation **F**ramework (SHELF)<sup>1</sup> is a package of documents, templates and software to carry out elicitation of probability distributions for uncertain quantities from a group of experts
- Two (most) common ways of elicitation are:
  1. Trial roulette method
  2. Quantile method
- Both then involve a least squares fit to a standard parametric distribution (usually)



# Calculating assurance

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- Once we have distributions for control,  $T$  and  $HR^*$  we can use these to calculate assurance
- For  $i = 1, \dots, M$ :
  - Simulate control data from  $p(\text{control})$
  - Sample  $T_i, HR_i^*$  from  $p(T), p(HR^*)$
  - Simulate treatment data from  $T_i, HR_i^*$
  - Simulate a clinical trial using control and treatment data
  - If trial successful then  $R_i = 1, 0$  otherwise
- End for
- Assurance is

Interim analyses (futility, efficacy..), choice of analysis (weighted log-rank test, RMST..) can be changed here

$$\frac{1}{M} \sum_{i=1}^M R_i$$



# DTE Shiny App (1/3)

## Assurance: Delayed Treatment Effects

[Control](#) [Eliciting the length of delay](#) [Eliciting the post-delay hazard ratio](#) [Feedback](#) [Calculating assurance](#) [Help](#)

Length of delay limits

0, 6

Length of delay values

2.5, 3, 3.5

Cumulative probabilities

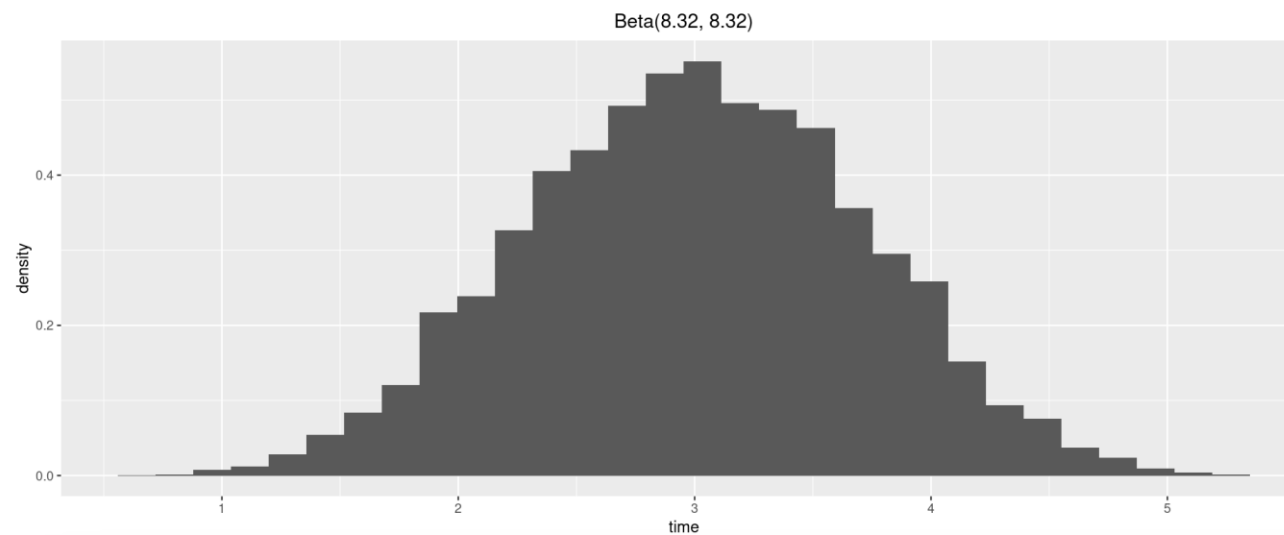
0.25, 0.5, 0.75

Distribution

Best fitting

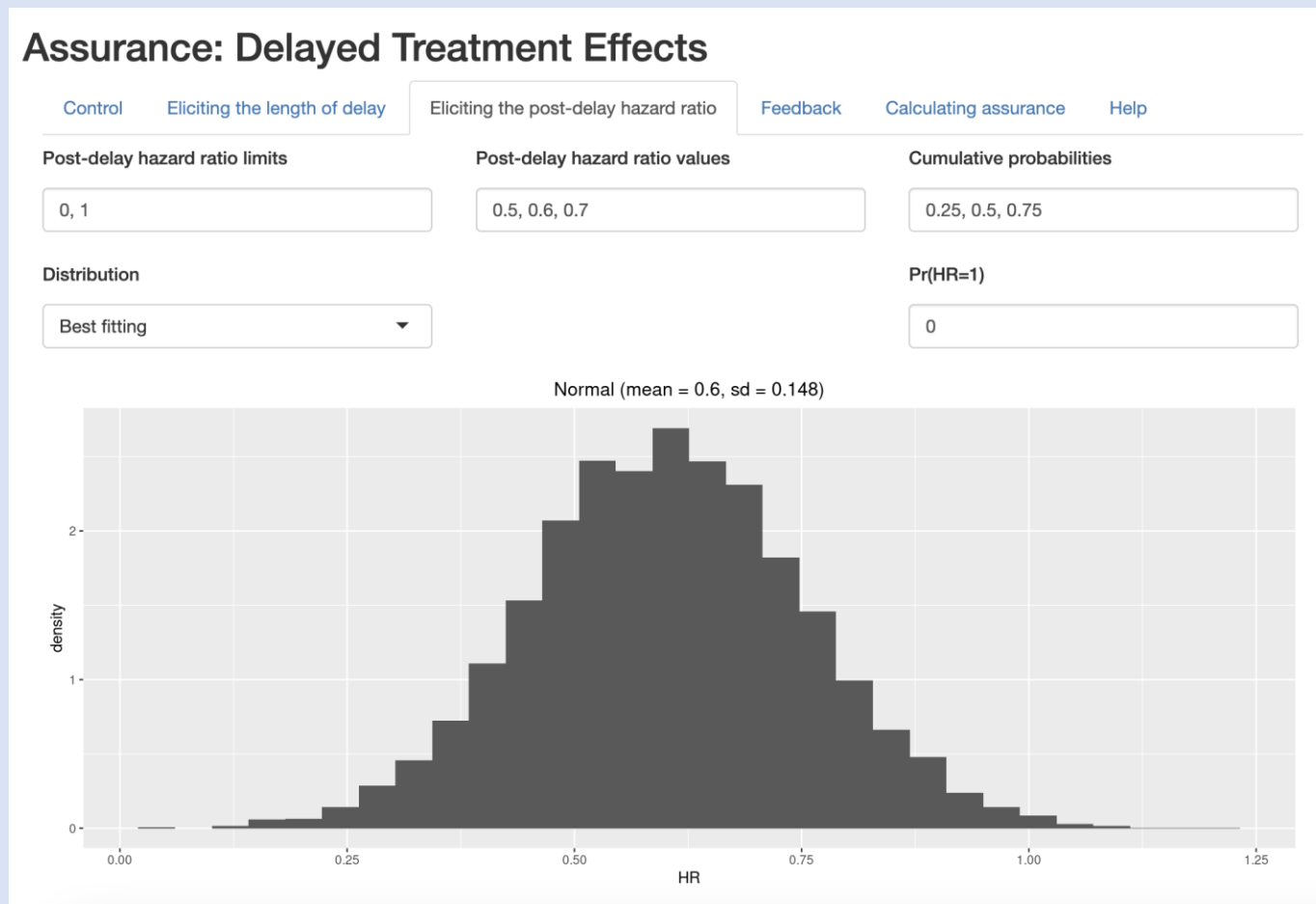
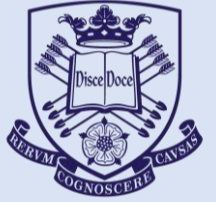
Pr(T=0)

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# DTE Shiny App (2/3)



# DTE Shiny App (3/3)



## Assurance: Delayed Treatment Effects

Control   Eliciting the length of delay   Eliciting the post-delay hazard ratio   Feedback   **Calculating assurance**   Help

Maximum number of patients in the trial

Recruitment length

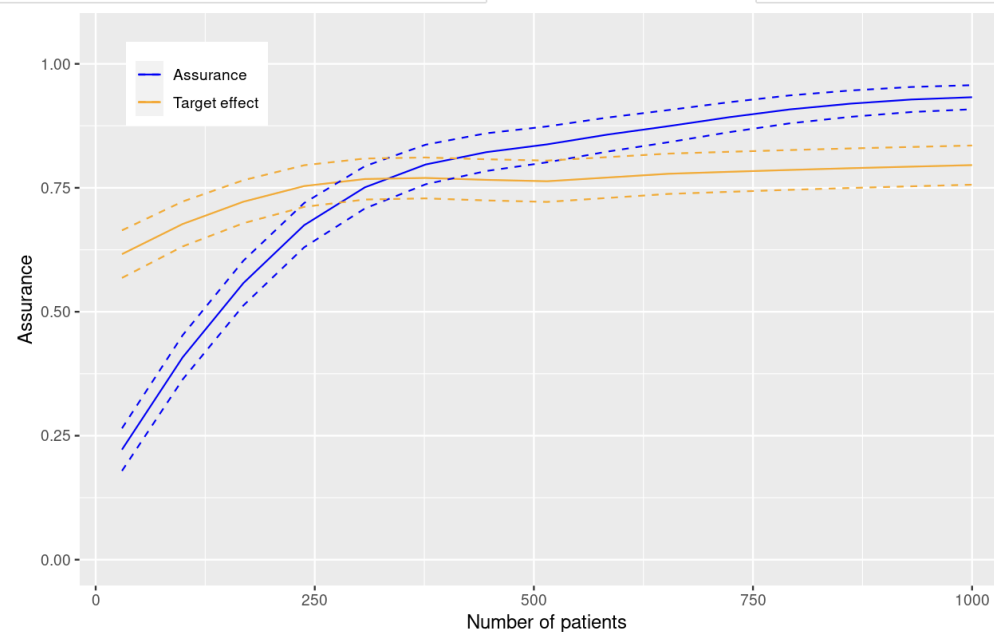
Ratio control

Ratio treatment

Maximum trial duration (including recruitment time)

Target effect (average hazard ratio)

Produce plot



The **blue** line is the proportion of trials that give rise to a 'successful' outcome.

The **orange** line is the proportion of trials in which the estimated average hazard ratio is less than the target effect - 0.8.

On average, 910 events are seen when 1000 patients are enrolled for 60 months.



# DTE assurance paper

arXiv > stat > arXiv:2310.06673

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Statistics > Applications

[Submitted on 10 Oct 2023]

## Assurance Methods for designing a clinical trial with a delayed treatment effect

James Salsbury, Jeremy Oakley, Steven Julious, Lisa Hampson

An assurance calculation is a Bayesian alternative to a power calculation. One may be performed to aid the planning of a clinical trial, specifically setting the sample size or to support decisions about whether or not to perform a study. Immuno-oncology (IO) is a rapidly evolving area in the development of anticancer drugs. A common phenomenon that arises from IO trials is one of delayed treatment effects, that is, there is a delay in the separation of the survival curves. To calculate assurance for a trial in which a delayed treatment effect is likely to be present, uncertainty about key parameters needs to be considered. If uncertainty is not considered, then the number of patients recruited may not be enough to ensure we have adequate statistical power to detect a clinically relevant treatment effect. We present a new elicitation technique for when a delayed treatment effect is likely to be present and show how to compute assurance using these elicited prior distributions. We provide an example to illustrate how this could be used in practice. Open-source software is provided for implementing our methods. Our methodology makes the benefits of assurance methods available for the planning of IO trials (and others where a delayed treatment effect is likely to occur).

Subjects: **Applications (stat.AP)**; Methodology (stat.ME)

Cite as: [arXiv:2310.06673](https://arxiv.org/abs/2310.06673) [stat.AP]  
(or [arXiv:2310.06673v1](https://arxiv.org/abs/2310.06673v1) [stat.AP] for this version)  
<https://doi.org/10.48550/arXiv.2310.06673>

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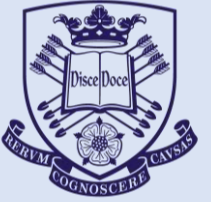
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# References

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# Thank you! Any questions?

*Arxiv paper*



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*DTE Shiny App*

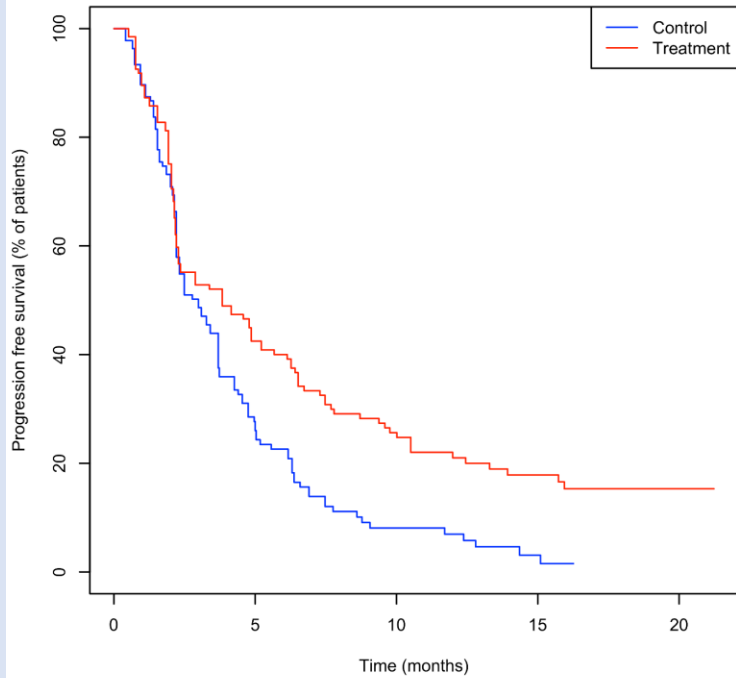
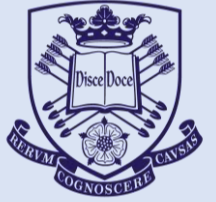


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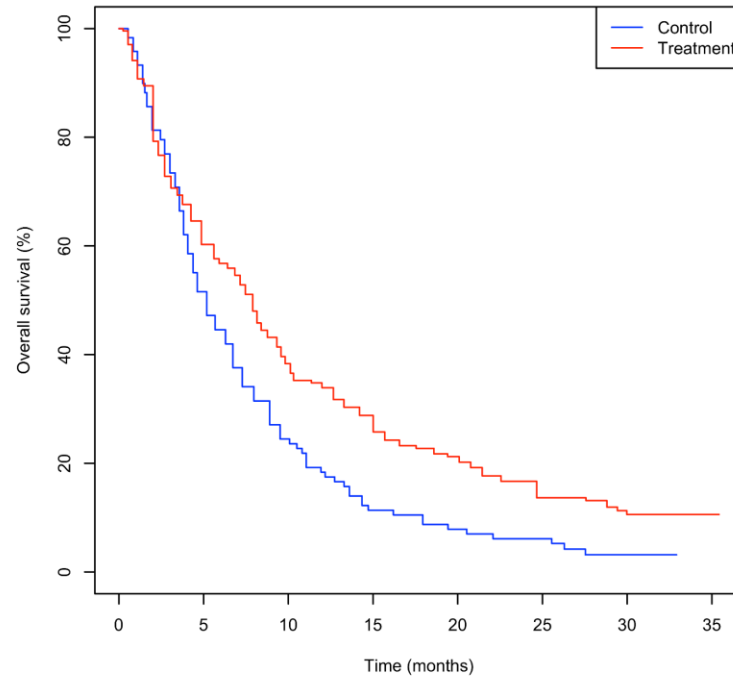


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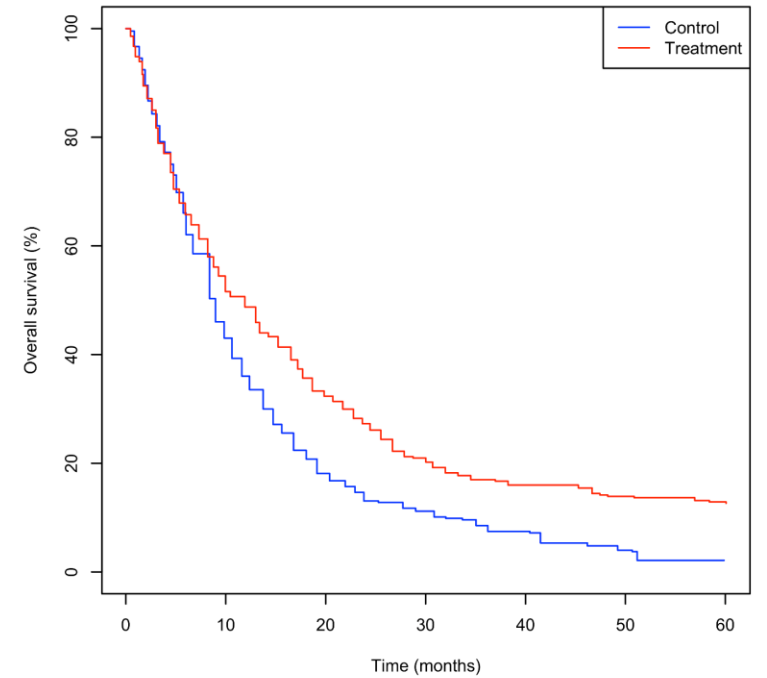
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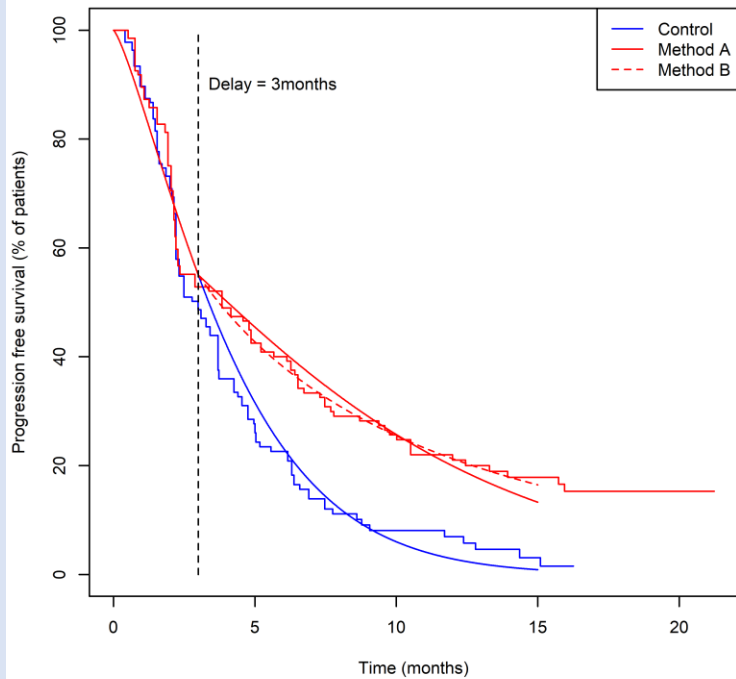


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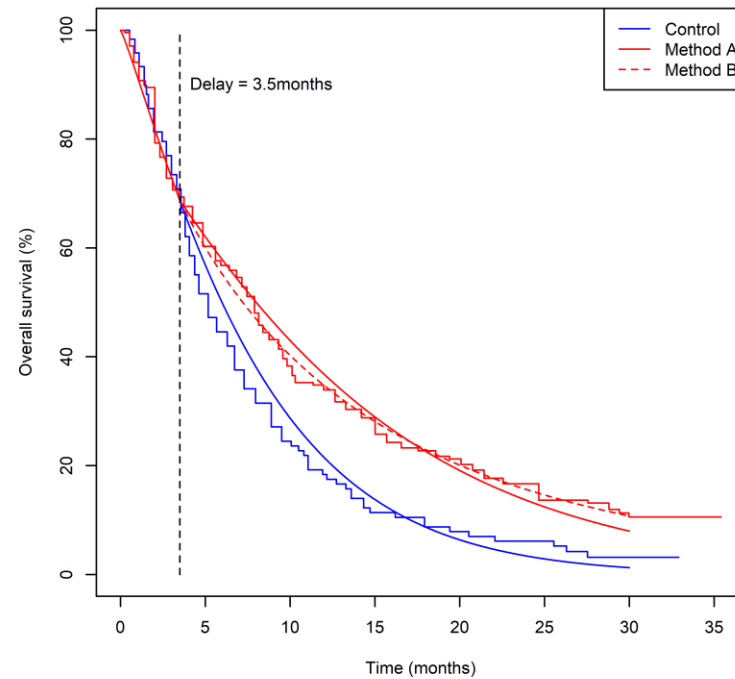


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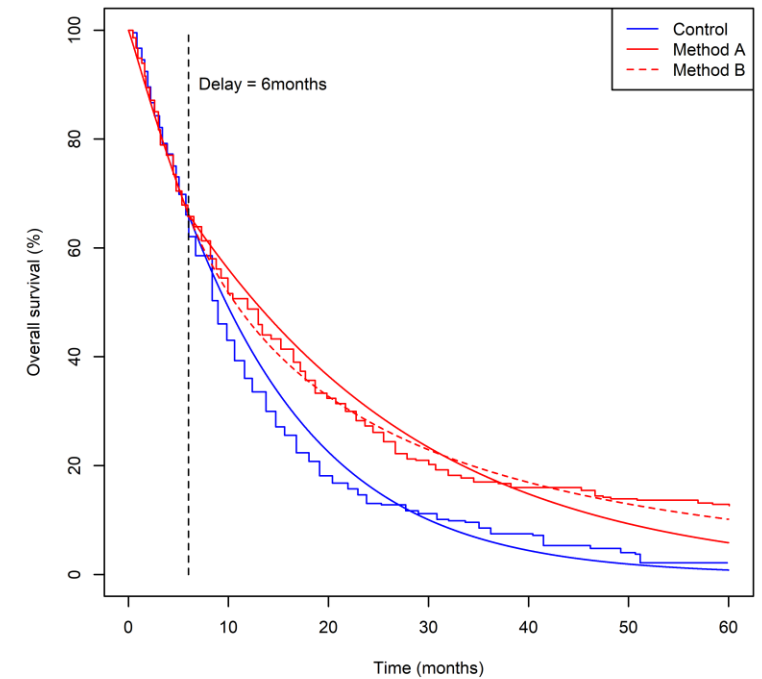
# Back-up slides



Checkmate 017



Checkmate 141



Checkmate 017 & Checkmate 057